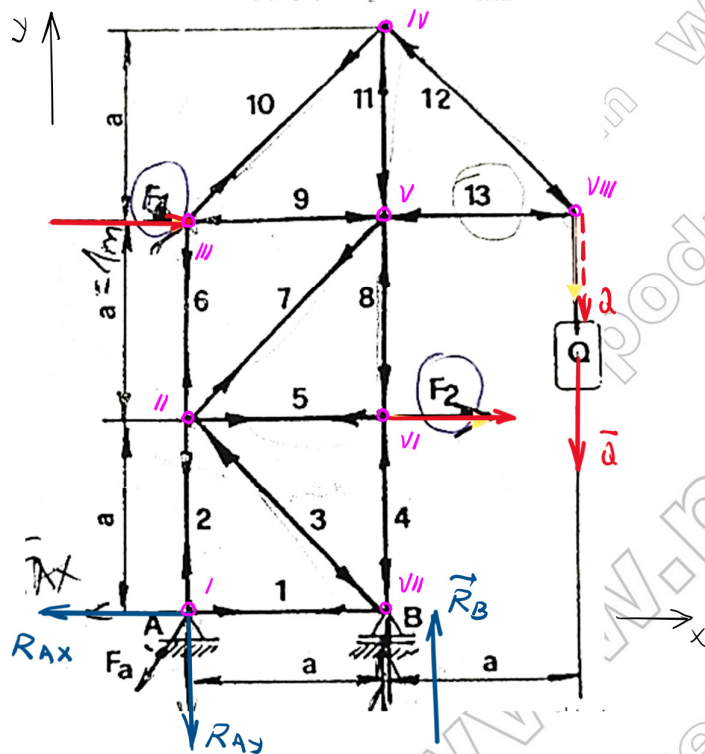


rešetkasti nosač djeluju dvije jednake sile:  $F_1 = F_2 = 500 \text{ N}$  i teret težine  $Q$ . Odredite otpore oslonaca u A i B i unutarnje sile u štapovima nosača, a)

$$Q = 100 \cdot X, X = 18 \Rightarrow Q = 1800 \text{ N}, F_1 = 500 \text{ N}, F_2 = 500 \text{ N}, a = 1 \text{ m}$$

### 1. Reakcije oslonaca



$$3 \text{ NV: } R_{AX}, R_{AY}, R_B$$

$$3 \text{ VR: } 1) \sum M_A = 0 \quad R_B = \dots$$

$$2) \sum M_B = 0 \quad R_{AY} = \dots$$

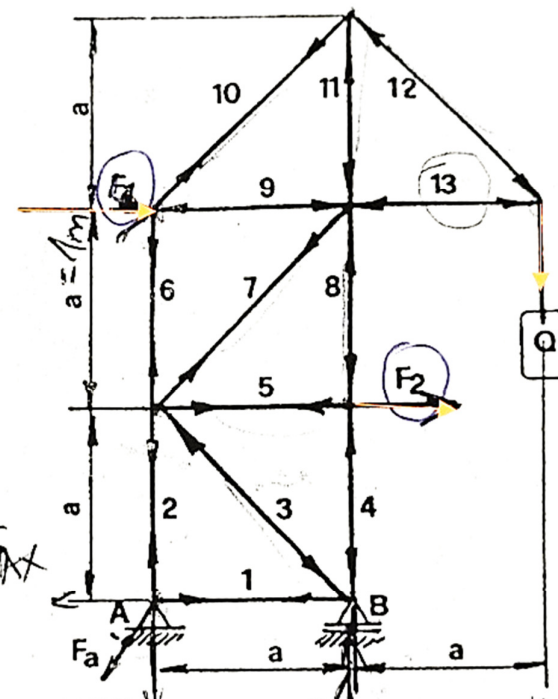
$$3) \sum F_{ix} = 0 \quad R_{AX} = \dots$$

$$1) \sum M_A = 0$$

$$-F_1 \cdot 2a - F_2 \cdot a + R_B \cdot a - Q \cdot 2a = 0 \quad (1) \quad | :a$$

$$R_B = 2F_1 + F_2 + 2Q$$

$$R_B = 2 \cdot 500 + 500 + 2 \cdot 1800$$



$$\underline{R_B = 5\ 100\ \text{N}}$$

$$2) \sum M_B = 0$$

$$R_{Ay} \cdot a - F_1 \cdot 2a - F_2 \cdot a - Q \cdot a = 0 \quad | :a \quad (2)$$

$$R_{Ay} = 2F_1 + F_2 + Q$$

$$R_{Ay} = 2 \cdot 500 + 500 + 1800$$

$$\underline{R_{Ay} = 3\ 300\ \text{N}}$$

$$3) \sum F_{ix} = 0$$

$$-R_{Ax} + F_1 + F_2 = 0 \quad (3)$$

$$R_{Ax} = F_1 + F_2$$

$$R_{Ax} = 500 + 500$$

$$\underline{R_{Ax} = 1000\ \text{N}}$$

2. Provjera ispravnosti reakcija oslonaca

$$\sum F_{iy} = 0$$

$$-R_{Ay} + R_B - Q = 0 \quad (4)$$

$$-3\ 300 + 5\ 100 - 1800 = 0$$

$$5\ 100 - 5\ 100 = 0$$

$$0 = 0$$

Reakcije su točne.

3. Otpor u osloncu A,  $R_A$

$$R_{Ax} \perp R_{Ay} \Rightarrow R_A = \sqrt{R_{Ax}^2 + R_{Ay}^2} \quad [\text{N}] \quad (5)$$

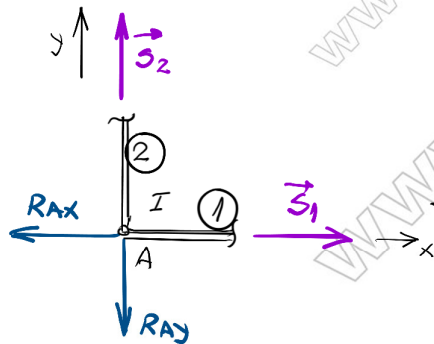
$$R_A = \sqrt{1000^2 + 3300^2}$$

$$\underline{R_A = 3\ 443,19\ \text{N}}$$

|       |       |       |       |       |       |       |       |       |          |          |          |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|----------|----------|----------|
| $S_1$ | $S_2$ | $S_3$ | $S_4$ | $S_5$ | $S_6$ | $S_7$ | $S_8$ | $S_9$ | $S_{10}$ | $S_{11}$ | $S_{12}$ | $S_{13}$ |
| ✓     | ✓     | ✓     | ✓     | ✓     | ✓     | ✓     | ✓     | ✓     | ✓        | ✓        | ✓        | ✓        |

#### 4. Sile u štapovima

##### 1) Ravnoteža čvora I



$$1) \sum F_{ix} = 0$$

$$S_1 - R_{AX} = 0 \quad (6)$$

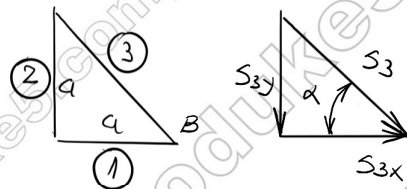
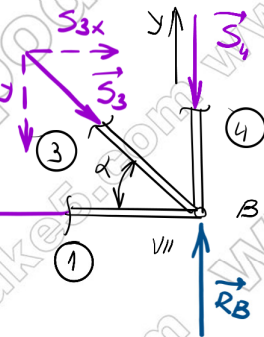
$$S_1 = 1000 \text{ N} \quad (\text{vlačna sila})$$

$$2) \sum F_{iy} = 0$$

$$S_2 - R_{AY} = 0 \quad (7)$$

$$S_2 = 3300 \text{ N} \quad (\text{VS})$$

##### 2) Ravnoteža čvora VII



$$\tan \alpha = \frac{a}{a} \quad (8)$$

$$\alpha = 45^\circ$$

$$1) \sum F_{ix} = 0$$

$$S_1 - S_{3x} = 0 \quad (9)$$

$$S_{3x} = S_3 \cdot \cos \alpha$$

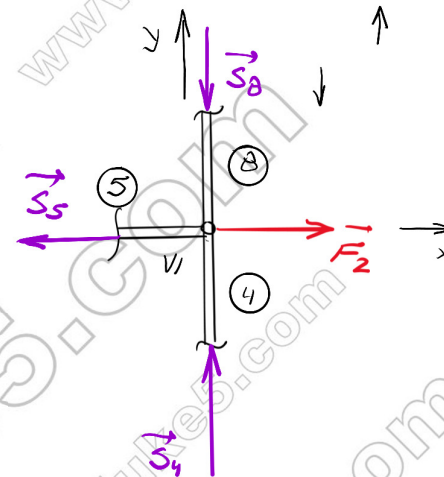
$$S_1 = S_3 \cos \alpha \quad | : \cos \alpha$$

$$S_3 = \frac{S_1}{\cos \alpha} \quad (10)$$

$$S_3 = \frac{1000}{\cos 45^\circ}$$

$$S_3 = 1414,21 \text{ N} \quad (\text{Tlačna sila})$$

##### 3) Ravnoteža čvora VI



$$1) \sum F_{ix} = 0$$

$$F_2 - S_5 = 0 \quad (13)$$

$$S_5 = 500 \text{ N} \quad (\text{VS})$$

$$2) \sum F_{iy} = 0$$

$$S_4 - S_8 = 0 \quad (14)$$

$$S_8 = 4100,00 \text{ N} \quad (\text{TS})$$

$$2) \sum F_{iy} = 0$$

$$R_B - S_4 - S_{3y} = 0 \quad (11)$$

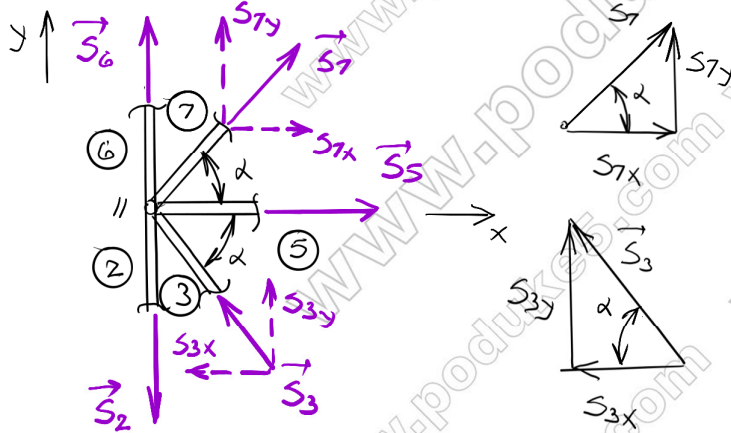
$$S_{3y} = S_3 \cdot \sin \alpha \quad (12)$$

$$S_4 = R_B - S_3 \cdot \sin \alpha \quad (13)$$

$$S_4 = 5100 - 1414,21 \cdot \sin 45^\circ$$

$$S_4 = 4100,00 \text{ N} \quad (\text{TS})$$

4) Ravnoteža čvora II



$$1) \sum F_{ix} = 0$$

$$S_5 + S_{7x} - S_{3x} = 0 \quad (15)$$

$$S_{7x} = S_7 \cos \alpha \quad (16)$$

$$S_{3x} = S_3 \cdot \cos \alpha \quad (17)$$

$$S_5 + S_7 \cos \alpha - S_3 \cos \alpha = 0$$

$$S_7 \cos \alpha = S_3 \cos \alpha - S_5 \quad | : \cos \alpha$$

$$S_7 = S_3 - \frac{S_5}{\cos \alpha}$$

$$S_7 = 1414,21 - \frac{500}{\cos 45^\circ}$$

$$S_7 = 707,10 \text{ N (vs)}$$

$$2) \sum F_{iy} = 0$$

$$S_6 - S_2 + S_{7y} + S_{3y} = 0 \quad (18)$$

$$S_{7y} = S_7 \cdot \sin \alpha$$

$$S_{3y} = S_3 \cdot \sin \alpha$$

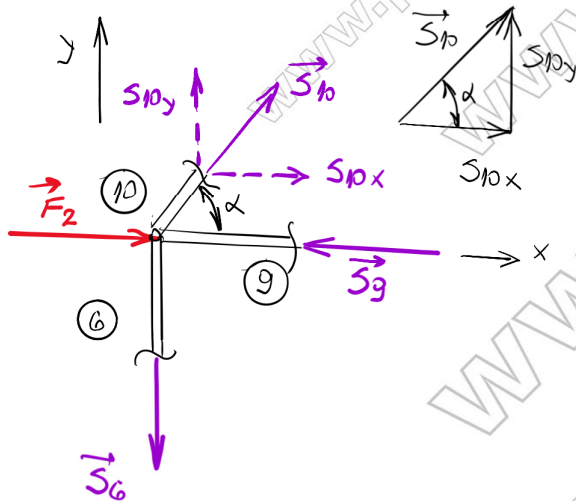
$$S_6 - S_2 + S_7 \sin \alpha + S_3 \sin \alpha = 0$$

$$S_6 = S_2 - S_7 \sin \alpha - S_3 \sin \alpha$$

$$S_6 = 3300 - \sin 45^\circ \cdot (707,1 + 1414,21)$$

$$S_6 = 1800,00 \text{ N (vs)}$$

5) Ravnoteža čvora III



$$1) \sum F_{ix} = 0$$

$$F_2 - S_9 + S_{10x} = 0 \quad (19)$$

$$S_{10x} = S_{10} \cdot \cos \alpha \quad (20)$$

$$F_2 - S_9 + S_{10} \cdot \cos \alpha = 0$$

$$S_9 = F_2 + S_{10} \cdot \cos \alpha \quad (23)$$

$$S_9 = 500 + 2545,58 \cdot \cos 45^\circ$$

$$S_9 = 2300 \text{ N (Ts)}$$

$$2) \sum F_{iy} = 0$$

$$S_{10y} - S_6 = 0 \quad (21)$$

$$S_{10y} = S_{10} \cdot \sin \alpha \quad (22)$$

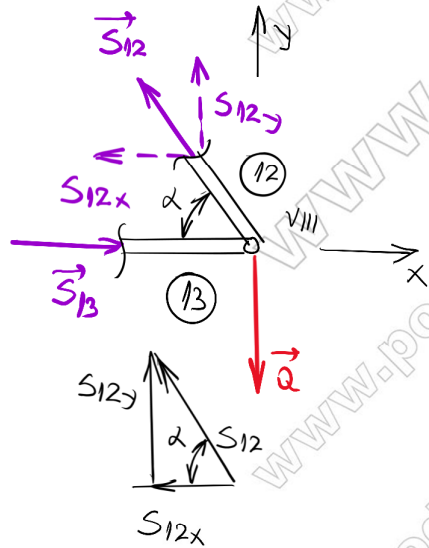
$$S_{10} \cdot \sin \alpha = S_6 \quad | : \sin \alpha$$

$$S_{10} = \frac{S_6}{\sin \alpha} \quad (23)$$

$$S_{10} = \frac{1800}{\sin 45^\circ}$$

$$S_{10} = 2545,58 \text{ N (vs)}$$

6) Ravnoteža čvora VIII



$$1) \sum F_{ix} = 0$$

$$S_{13} - S_{12x} = 0 \quad (24)$$

$$S_{12x} = S_{12} \cdot \cos \alpha \quad (25)$$

$$S_{13} = S_{12} \cdot \cos \alpha \quad (26)$$

$$S_{13} = 2545,58 \cdot \cos 45^\circ$$

$$S_{13} = 1800 \text{ N} \quad (25)$$

$$2) \sum F_{iy} = 0$$

$$S_{12y} - Q = 0 \quad (27)$$

$$S_{12y} = S_{12} \cdot \sin \alpha \quad (28)$$

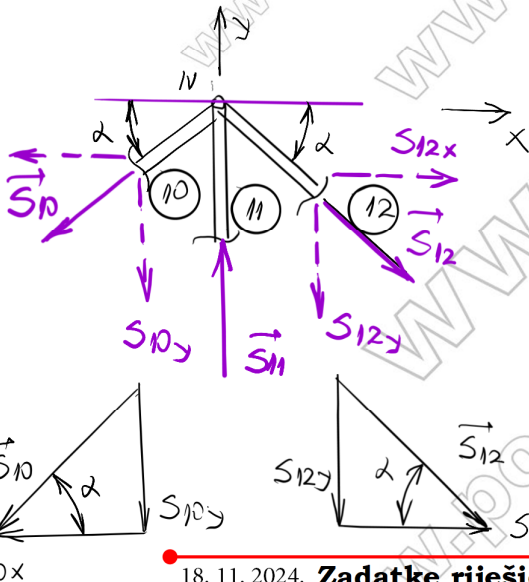
$$Q = S_{12} \cdot \sin \alpha \quad | : \sin \alpha$$

$$S_{12} = \frac{Q}{\sin \alpha} \quad (29)$$

$$S_{12} = \frac{1800}{\sin 45^\circ}$$

$$S_{12} = 2545,58 \text{ N} \quad (15)$$

7) Ravnoteža čvora IV



Od ranije izračunato:

$$S_{10} = 2545,58 \text{ N} \quad (15)$$

$$S_{12} = 2545,58 \text{ N} \quad (15)$$

Provjera sila u štapovima:

$$\sum F_{ix} = 0$$

$$S_{12} \cdot \cos \alpha - S_{10} \cdot \cos \alpha = 0 \quad (30)$$

Ispunjeno  $\Rightarrow$  sile u štapovima su točne

$$\sum F_{iy} = 0$$

$$S_{11} - S_{12y} - S_{10y} = 0 \quad (31)$$

$$S_{10y} = S_{10} \cdot \sin \alpha \quad (32)$$

$$S_{12y} = S_{12} \cdot \sin \alpha \quad (33)$$

$$S_{11} = S_{12} \sin \alpha + S_{10} \sin \alpha$$

$$S_{11} = 2 \cdot 545,50 \cdot \sin 45^\circ + 2 \cdot 545,50 \cdot \sin 45^\circ$$

$$\underline{S_{11} = 3600 \text{ N (Ts)}}$$